

Name Answer key

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**Honors Alg. 2, Term 3, Quiz 2 Exponent Rules and Dividing Polynomials**

Write each polynomial in standard form. Then classify it by its degree and by the number of terms.

1.  $f(m) = 4m^2 + 7m^4$  (3)

$f(m) = 7m^4 + 4m^2$

D: 4

binomial

2.  $f(t) = 4t + 3t^3 + 2t - 7$  (3)

$f(t) = 3t^3 + 6t - 7$

D: 3

trinomial

3.  $f(xy) = 6xy + 5x^2y + 3x^3y^2$  (3)

$f(xy) = 3x^3y^2 + 5x^2y + 6xy$

Degree: 5

trinomial

Divide by long division.

4.  $\frac{x^3 - 1}{x + 2}$  (4)

$$\begin{array}{r} x^2 - 2x + 4 \\ x + 2 \overline{) x^3 - 1} \\ \underline{-x^3 + 2x^2} \phantom{-1} \\ -2x^2 - 1 \\ \underline{+2x^2 + 4x} \\ 4x - 1 \\ \underline{-4x + 8} \\ -9 \end{array}$$

5.  $(2x^4 - 9x^3 + 21x^2 - 26x + 12)(2x - 3)^{-1}$  (4)

$$\begin{array}{r} x^3 - 3x^2 + 6x - 4 \\ 2x - 3 \overline{) 2x^4 - 9x^3 + 21x^2 - 26x + 12} \\ \underline{-(2x^4 + 3x^3)} \\ -6x^3 + 21x^2 \\ \underline{-(-6x^3 + 9x^2)} \\ 12x^2 - 26x \\ \underline{-(12x^2 + 18x)} \\ -8x + 12 \\ \underline{-(-8x + 12)} \\ 0 \end{array}$$

$$\boxed{\begin{array}{r} x^2 - 2x + 4 - 9 \\ \hline x + 2 \end{array}}$$

Divide by synthetic division.

6.  $\frac{3x^3 - 6x + 12}{x - 2}$  (3)

$$\begin{array}{r|rrrrr} 2 & 3 & 0 & -6 & 12 & \\ & \downarrow & 6 & 12 & 12 & \\ \hline & 3 & 6 & 6 & 24 & \end{array}$$

$$\boxed{\begin{array}{r} 3x^2 + 6x + 6 + 24 \\ \hline x - 2 \end{array}}$$

7.  $2x - 1 \mid 2x^4 + 3x^3 - 4x^2 + x + 1$  (4)

$$\begin{array}{r} x - \frac{1}{2} \overline{) x^4 + \frac{3}{2}x^3 - 2x^2 + \frac{1}{2}x + \frac{1}{2}} \\ \hline \frac{1}{2} \mid \begin{array}{r} 1 \quad \frac{3}{2} \quad -2 \quad \frac{1}{2} \quad \frac{1}{2} \\ \downarrow \quad \frac{1}{2} \quad 1 \quad -\frac{1}{2} \quad 0 \\ \hline 1 \quad 2 \quad -1 \quad 0 \quad \frac{1}{2} \end{array} \end{array}$$

$$\boxed{\begin{array}{r} x^3 + 2x^2 - x + \frac{1}{2} \\ \hline x - \frac{1}{2} \end{array}}$$

Simplify the expression.

8.  $\frac{(3xy)^2(4x^2y^2)^2}{-36x^7y^2}$

$$\frac{9x^2y^2 \cdot 16x^4y^4}{-36x^7y^2}$$

$$\frac{144x^6y^6}{-36x^7y^2}$$

$$\frac{-4y^4}{x}$$

9.  $(3y^3 + 2y + 1) \div 3y$

$$\frac{3y^3}{3y} + \frac{2y}{3y} + \frac{1}{3y}$$

$$y^2 + \frac{2}{3} + \frac{1}{3y}$$

**Word Problems:**

10. Identify the errors in planning the solution or solving the problem. Then write the correct solution.

Use polynomial division to divide  $x^4 + x^3 - 7x - 3$  by  $x + 3$ . What is the quotient and remainder?

$$\begin{array}{r} x^3 - 2x^2 - 1 \\ x + 3 \overline{) x^4 + 1x^3 - 7x - 3} \\ \underline{-x^4 + 3x^3} \phantom{- 7x - 3} \\ -2x^3 - 7x \phantom{- 3} \\ \underline{-2x^3 - 6x^2} \phantom{- 3} \\ -1x - 3 \\ \underline{-1x - 3} \\ 0 \end{array}$$

they didnt make x  
~~3x^2 + 0~~

$$\begin{array}{r} x^3 - 2x^2 + 6x - 25 \\ x + 3 \overline{) x^4 + x^3 - 7x - 3} \\ \underline{7x^4 - 3x^3} \phantom{- 7x - 3} \\ -2x^3 - 7x \phantom{- 3} \\ \underline{+ 2x^3 + 6x^2} \phantom{- 3} \\ +6x^2 - 7x \phantom{- 3} \\ \underline{-6x^2 + 18x} \phantom{- 3} \\ -25x - 3 \\ \underline{+ 25x + 75} \\ 72 \end{array}$$

The quotient is  $x^3 - 2x^2 - 1$  with remainder 0.

$$\frac{x^3 - 2x^2 + 6x - 25 + 72}{x + 3}$$

11. The expression  $V(x) = x^3 - 13x + 12$  represents the volume of a rectangular safe in cubic feet. The length of the safe is  $x + 4$ . What linear expressions with integer coefficients could represent the other dimensions of the safe? Assume that the height is greater than the width.

$$\begin{array}{r} 4 \overline{) 1 \ 0 \ -13 \ 12} \\ \underline{4 \ 16 \ -12} \\ 1 \ -4 \ 3 \ 0 \end{array}$$

$$x^2 - 4x + 3$$

$$(x-1)(x-3)$$