

$$x = 8, y = 15$$

$$r = \sqrt{x^2 + y^2} = \sqrt{8^2 + 15^2} = \sqrt{289} = 17$$

$$3. \quad \sin \theta = \frac{y}{r} = \frac{15}{17} \qquad \csc \theta = \frac{r}{y} = \frac{17}{15}$$

$$\cos \theta = \frac{x}{r} = \frac{8}{17} \qquad \sec \theta = \frac{r}{x} = \frac{17}{8}$$

$$\tan \theta = \frac{y}{x} = \frac{15}{8} \qquad \cot \theta = \frac{x}{y} = \frac{8}{15}$$

$$x = -7, y = -24$$

$$r = \sqrt{x^2 + y^2} = \sqrt{(-7)^2 + (-24)^2} = \sqrt{625} = 25$$

$$\sin \theta = \frac{y}{r} = \frac{-24}{25} = -\frac{24}{25}$$

$$\cos \theta = \frac{x}{r} = \frac{-7}{25} = -\frac{7}{25}$$

$$5. \quad \tan \theta = \frac{y}{x} = \frac{-24}{-7} = \frac{24}{7}$$

$$\csc \theta = \frac{r}{y} = \frac{25}{-24} = -\frac{25}{24}$$

$$\sec \theta = \frac{r}{x} = \frac{25}{-7} = -\frac{25}{7}$$

$$\cot \theta = \frac{x}{y} = \frac{-7}{-24} = \frac{7}{24}$$

$$x = 2, y = -2$$

$$r = \sqrt{x^2 + y^2} = \sqrt{2^2 + (-2)^2} = \sqrt{8} = 2\sqrt{2}$$

$$\sin \theta = \frac{y}{r} = \frac{-2}{2\sqrt{2}} = -\frac{1}{\sqrt{2}} = -\frac{\sqrt{2}}{2}$$

$$\cos \theta = \frac{x}{r} = \frac{2}{2\sqrt{2}} = \frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2}$$

7.  $\tan \theta = \frac{y}{x} = \frac{-2}{2} = -1$

$$\csc \theta = \frac{r}{y} = \frac{2\sqrt{2}}{-2} = -\sqrt{2}$$

$$\sec \theta = \frac{r}{x} = \frac{2\sqrt{2}}{2} = \sqrt{2}$$

$$\cot \theta = \frac{x}{y} = \frac{2}{-2} = -1$$

$$x = -3, y = -5$$

$$r = \sqrt{x^2 + y^2} = \sqrt{(-3)^2 + (-5)^2} = \sqrt{34}$$

$$\sin \theta = \frac{y}{r} = \frac{-5}{\sqrt{34}} = -\frac{5\sqrt{34}}{34}$$

$$\cos \theta = \frac{x}{r} = \frac{-3}{\sqrt{34}} = -\frac{3\sqrt{34}}{34}$$

9.  $\tan \theta = \frac{y}{x} = \frac{-5}{-3} = \frac{5}{3}$

$$\csc \theta = \frac{r}{y} = \frac{\sqrt{34}}{-5} = -\frac{\sqrt{34}}{5}$$

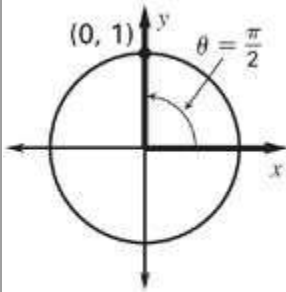
$$\sec \theta = \frac{r}{x} = \frac{\sqrt{34}}{-3} = -\frac{\sqrt{34}}{3}$$

$$\cot \theta = \frac{x}{y} = \frac{-3}{-5} = \frac{3}{5}$$

C;

11.  $x = -7, y = -4$

$$\tan \alpha = \frac{y}{x} = \frac{-4}{-7} = \frac{4}{7}$$



13.  $x = 0, y = 1, r = 1$

$$\sin \theta = \frac{y}{r} = \frac{1}{1} = 1$$

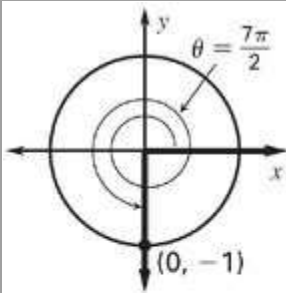
$$\csc \theta = \frac{r}{y} = \frac{1}{1} = 1$$

$$\cos \theta = \frac{x}{r} = \frac{0}{1} = 0$$

$$\sec \theta = \frac{r}{x} = \frac{1}{0} \text{ undefined}$$

$$\tan \theta = \frac{y}{x} = \frac{1}{0} \text{ undefined}$$

$$\cot \theta = \frac{x}{y} = \frac{0}{1} = 0$$



15.  $x = 0, y = -1, r = 1$

$$\sin \theta = \frac{y}{r} = \frac{-1}{1} = -1$$

$$\csc \theta = \frac{r}{y} = \frac{1}{-1} = -1$$

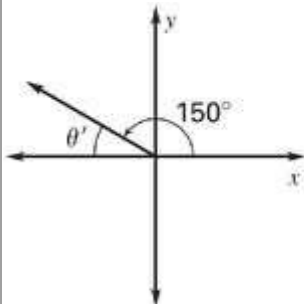
$$\cos \theta = \frac{x}{r} = \frac{0}{1} = 0$$

$$\sec \theta = \frac{r}{x} = \frac{1}{0} \text{ undefined}$$

$$\tan \theta = \frac{y}{x} = \frac{-1}{0} \text{ undefined}$$

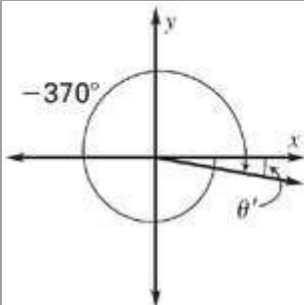
$$\cot \theta = \frac{x}{y} = \frac{0}{-1} = 0$$

17.



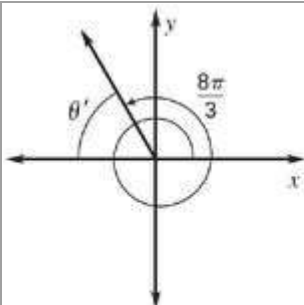
The terminal side of  $\theta$  lies in Quadrant II.  
So,  $\theta' = 180^\circ - 150^\circ = 30^\circ$ .

19.



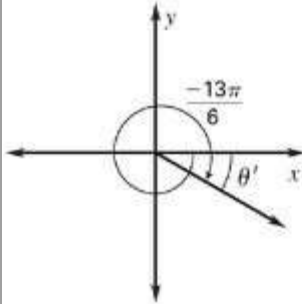
$\theta$  is coterminal with  $350^\circ$ , whose terminal side lies in Quadrant IV. So,  $\theta' = 360^\circ - 350^\circ = 10^\circ$ .

21.



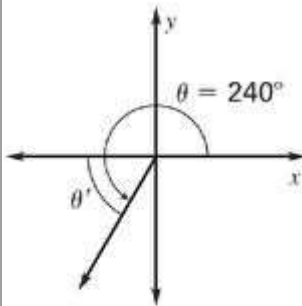
$\theta$  is coterminal with  $\frac{2\pi}{3}$ , whose terminal side lies in Quadrant II. So,  $\theta' = \pi - \frac{2\pi}{3} = \frac{\pi}{3}$ .

23.



$\theta$  is coterminal with  $\frac{11\pi}{6}$ , whose terminal side lies in Quadrant IV. So,  $\theta' = 2\pi - \frac{11\pi}{6} = \frac{\pi}{6}$ .

25.

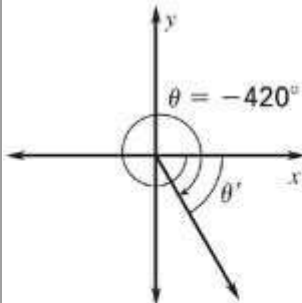


$$\theta' = 240^\circ - 180^\circ = 60^\circ.$$

Tangent is positive in Quadrant III.

$$\text{So, } \tan 240^\circ = \tan 60^\circ = \sqrt{3}.$$

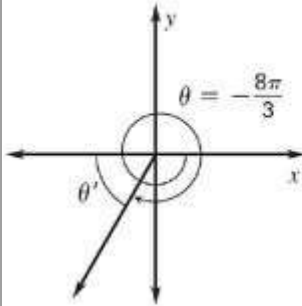
27.



$$\theta \text{ is coterminal with } 300^\circ. \text{ So, } \theta' = 360^\circ - 300^\circ = 60^\circ.$$

Cosecant is negative in Quadrant IV.

$$\text{So, } \csc(-420^\circ) = -\csc 60^\circ = -\frac{2\sqrt{3}}{3}.$$

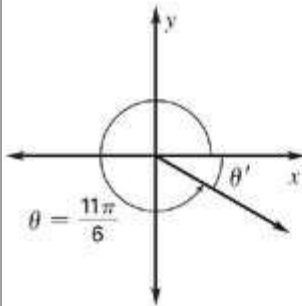


29.

$\theta$  is coterminal with  $\frac{4\pi}{3}$ . So,  $\theta' = \frac{4\pi}{3} - \pi = \frac{\pi}{3}$ .

Cotangent is positive in Quadrant III.

$$\text{So, } \cot\left(-\frac{8\pi}{3}\right) = \cot\left(\frac{\pi}{3}\right) = \frac{\sqrt{3}}{3}.$$



31.

$$\theta' = 2\pi - \frac{11\pi}{6} = \frac{\pi}{6}.$$

Secant is positive in Quadrant IV.

$$\text{So, } \sec\frac{11\pi}{6} = \sec\frac{\pi}{6} = \frac{2\sqrt{3}}{3}.$$